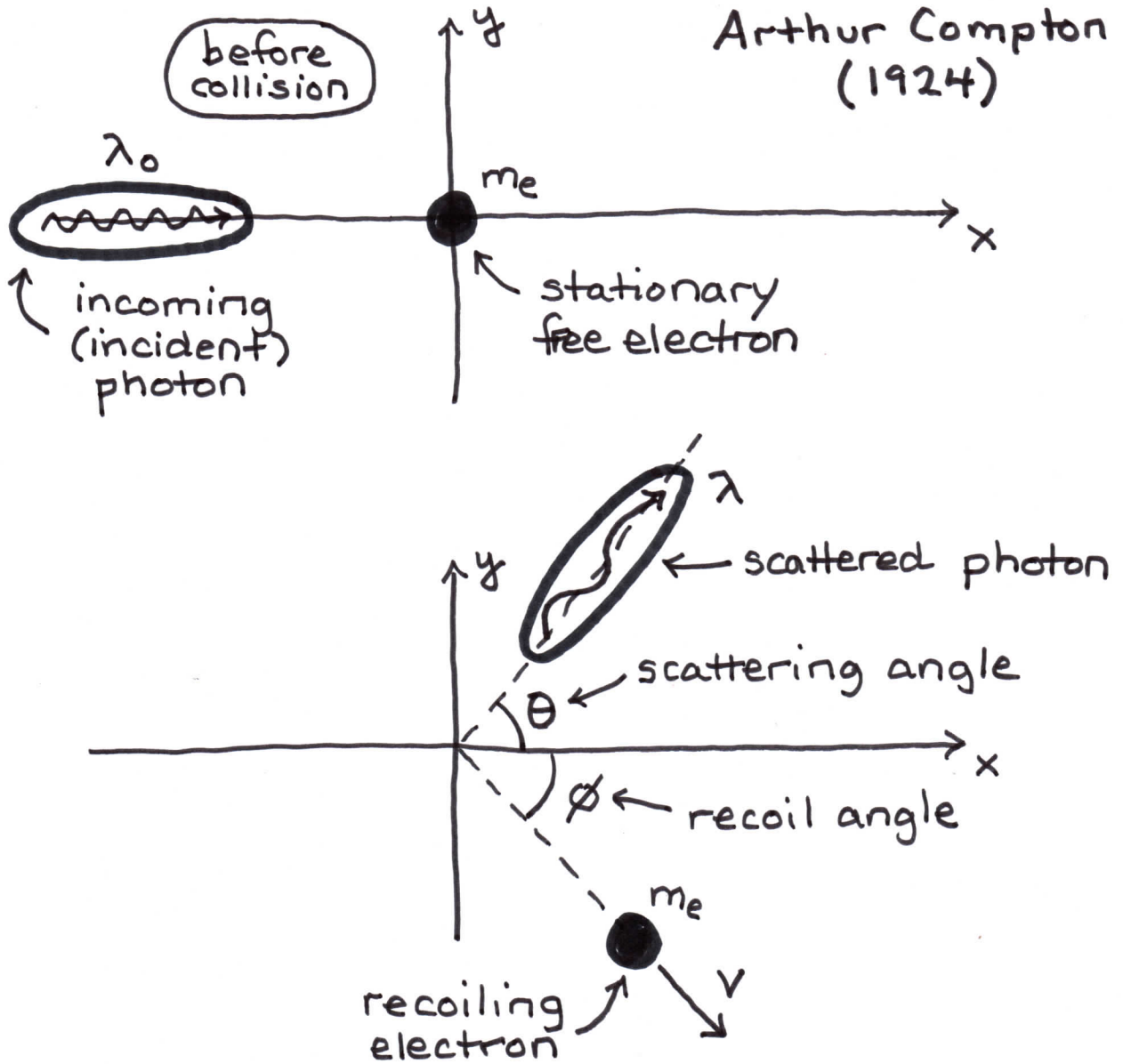


Compton Scattering



$$\lambda = \lambda_0 + \frac{h}{m_e c} (1 - \cos \theta)$$

called the Compton wavelength of the electron $\leftarrow \lambda_C = .00243 \text{ nm}$



"After long reflection in so and meditation, I suddenly the idea, during the year 1 that the discovery made by Einstein in 1905 should be generalised by extending it all material particles and notably to electrons."

Louis-Victor de Broglie

de Broglie's Hypothesis

Whenever a particle has a momentum p , its motion is associated with ("guided by") a wave whose wavelength is

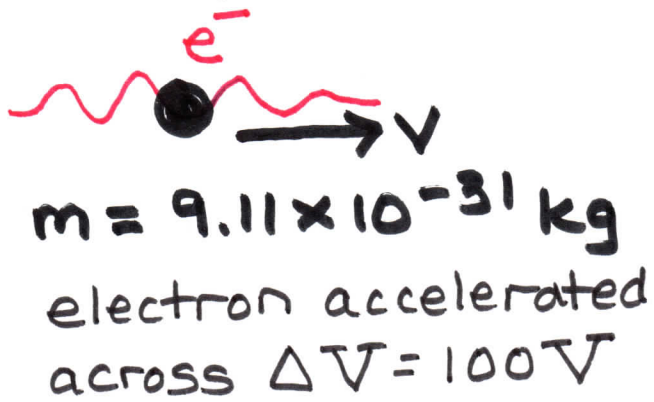
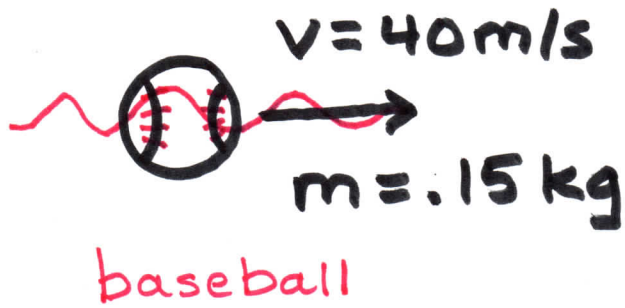
$$\lambda = \frac{h}{p}$$

from his
1924
dissertation

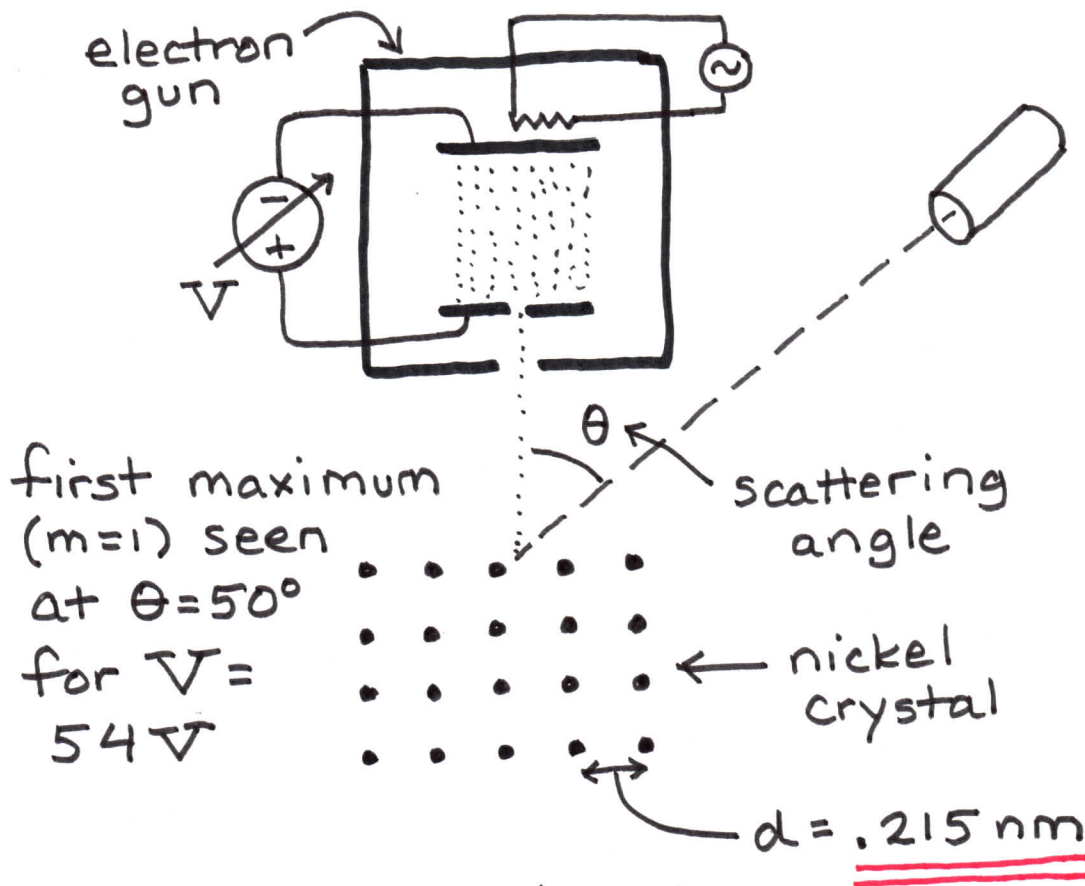
(1924)

Planck's constant
 $6.63 \times 10^{-34} \text{ J}\cdot\text{s}$

de Broglie Wavelength



Davisson-Germer Experiment



$$\begin{aligned}
 m\lambda &= d \sin \theta \\
 \lambda &= \frac{d \sin \theta}{m} \\
 &= \frac{.215 \text{ nm} (\sin 50^\circ)}{1} \\
 &= \boxed{.165 \text{ nm}}
 \end{aligned}$$

$$\begin{aligned}
 \lambda_{dB} &= \frac{h}{p} = \frac{h}{\sqrt{2m_e K}} \\
 &= \frac{hc}{\sqrt{2m_e c^2 K}} \\
 &= \frac{1240 \text{ eV} \cdot \text{nm}}{\sqrt{2(511,000 \text{ eV})(54 \text{ eV})}} \\
 &= \boxed{.167 \text{ nm}}
 \end{aligned}$$

1927

Lester
Germer

Clinton
Joseph
Davisson

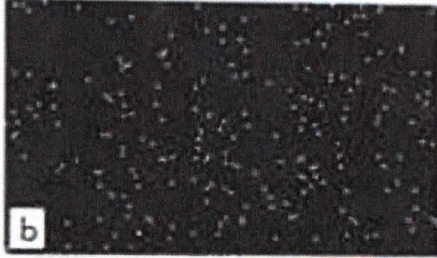


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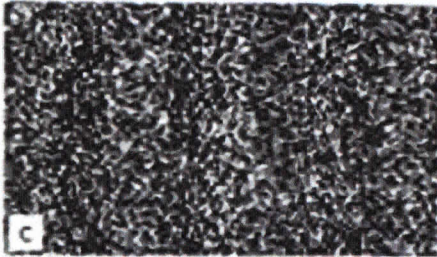
2 slit Electron Diffraction



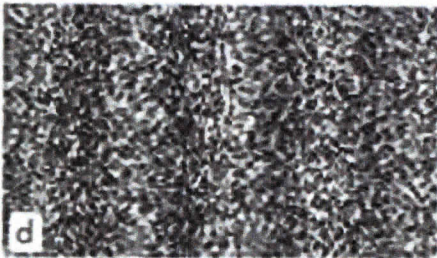
a) After firing a few individual electrons towards the two slits, we detect the arrival of each one.



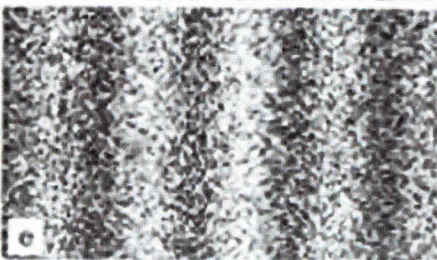
b) After a few hundred electrons, there is still not a clear interference pattern.



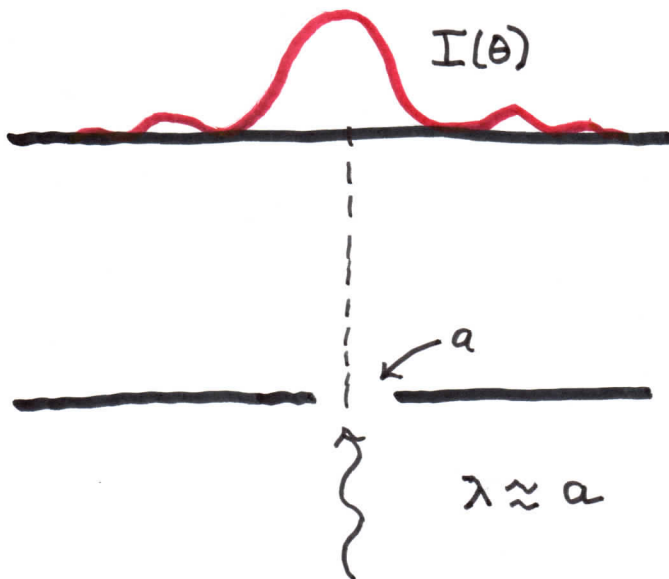
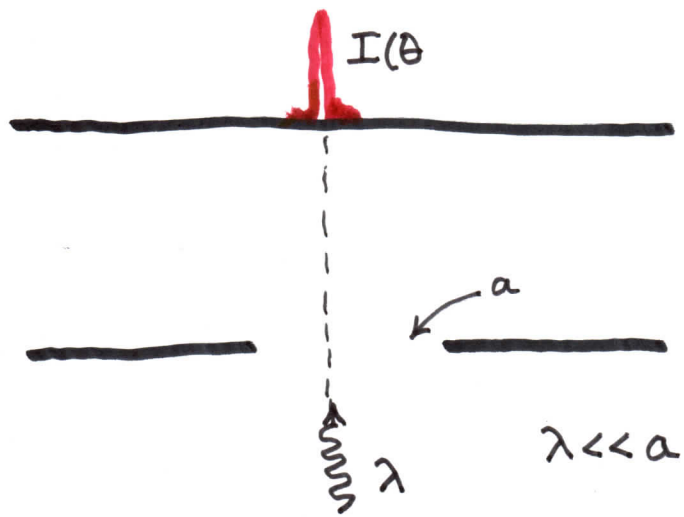
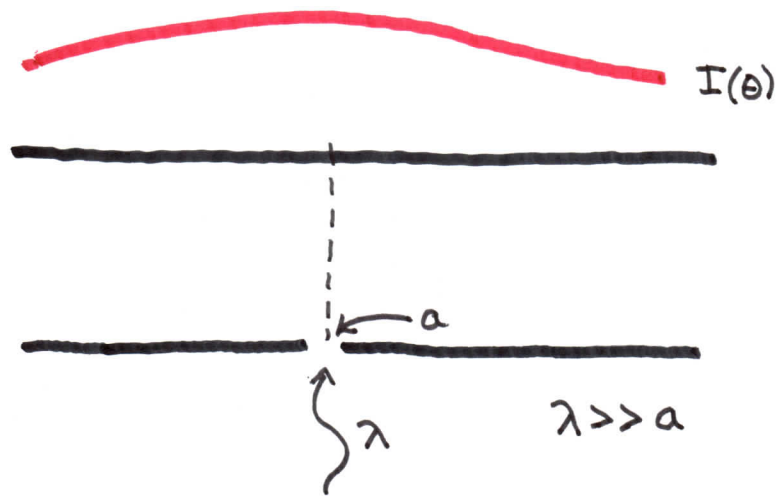
c) After thousands of electrons, a clear pattern emerges.



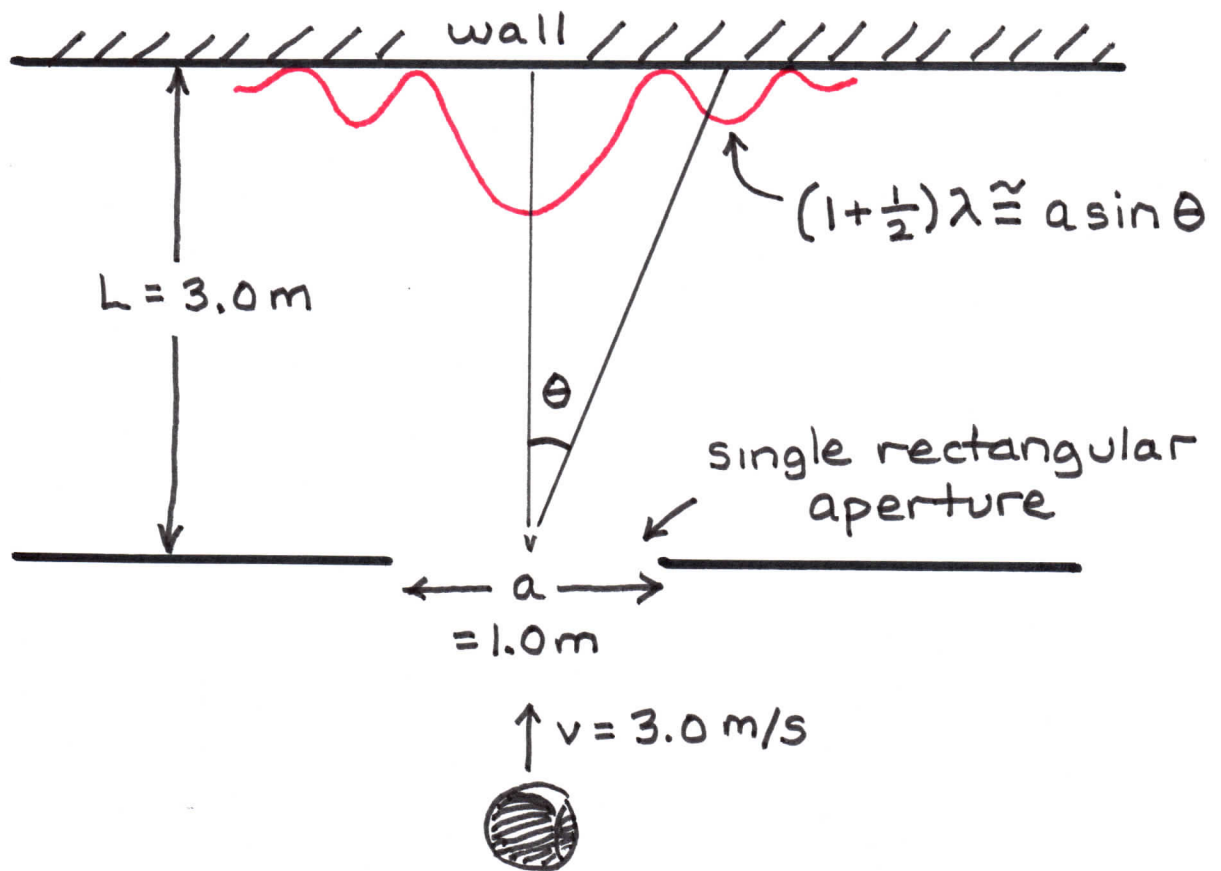
d) After many thousands of electrons, the pattern is better defined.



e) As we keep firing electrons, the pattern gets more and more sharp.



Diffraction Through a Door



Heisenberg Uncertainty Principle

W. Heisenberg (1927)

* It is impossible to know simultaneously an object's exact position and momentum.

$$X = 1.395 \text{ nm} \pm .005 \text{ nm}$$



$x \pm \Delta x$ ← uncertainty in x-position

$p_x \pm \Delta p_x$ ← uncertainty in x-momentum

$$\Delta p_x \Delta x \geq \frac{h}{4\pi}$$

$$\Delta E \Delta t \geq \frac{h}{4\pi}$$

example

e^-
electron $\rightarrow v = 300 \text{ m/s} \pm .03 \text{ m/s}$

$$p = mv = 9.11 \times 10^{-31} \text{ kg} (300 \text{ m/s} \pm .03 \text{ m/s})$$

$$= 2.73 \times 10^{-28} \text{ kgm/s} \pm 2.73 \times 10^{-32} \text{ kgm/s}$$

\uparrow
 Δp_x

$$\Delta x_{\text{best}} = \Delta x_{\text{min}} = \frac{h}{4\pi \Delta p_x}$$

$$= \frac{6.63 \times 10^{-34} \text{ J}\cdot\text{s}}{4\pi (2.73 \times 10^{-32} \text{ kgm/s})} = \boxed{1.93 \text{ nm}}$$

Google "Richard Feynman on
Electron 2 Slit Experiment"

find youtube video

Richard Feynman
lecture: Fall 1964
Cornell University

→ [youtube.com/watch?v=citY6G8ePJw](https://www.youtube.com/watch?v=citY6G8ePJw)